

Width-Integrals of Mixed Projection Bodies and Mixed Affine Surface Area ¹

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Abstract

The main purposes of this paper are to establish some new Brunn-Minkowski inequalities for width-integrals of mixed projection bodies and affine surface area of mixed bodies, and get their inverse forms.

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