Solution of a Recursive Sequence of Order Ten [1]

E. M. Elsayed

Abstract

We obtain in this paper the solutions of the following rational non-linear difference equations

$$x_{n+1} = \frac{x_{n-9}}{\pm 1 \pm x_{n-4} x_{n-9}}, \quad n = 0, 1, ...,$$

where initial values are non zero real numbers.

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Elsayed M. Elsayed
King AbdulAziz University, Faculty of Science
Department of Mathematics
P. O. Box 80203, Jeddah 21589, Saudi Arabia.

Permanent address:
Mansoura University, Faculty of Science
Department of Mathematics
Mansoura 35516, Egypt.
e-mail: emelsayed@mans.edu.eg, emmelsayed@yahoo.com.