SUBORDINATION AND SUPERORDINATION FOR CERTAIN ANALYTIC FUNCTIONS CONTAINING FRACTIONAL INTEGRAL

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Abstract. The purpose of the present article is to derive some subordination and superordination results for certain normalized analytic functions involving fractional integral operator. Moreover, this result is applied to find a relation between univalent solutions for fractional differential equation.

Full text

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