

## ULAM-HYERS STABILITY OF FIXED POINT EQUATIONS FOR MULTIVALUED OPERATORS ON $KST$ SPACES

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**Abstract.** In this paper we define the notions of Ulam-Hyers stability on  $KST$  spaces and  $c_w$ -weakly Picard operator for the multivalued operators case in order to establish a relation between these.

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