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## POSITIVE DEFINITENESS, REPRODUCING KERNEL HILBERT SPACES AND BEYOND

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ABSTRACT. Positive definiteness, reproducing kernel Hilbert spaces, integral operators and Mercer's theorem in its various formats are common topics in many branches of mathematics. In this paper we review and upgrade upon some recent results that always involve at least two of them and indicate a few directions in which additional research could be carried out.

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