

GROUPOID C^* -ALGEBRAS

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Abstract. The purpose of this paper is to recall the main ingredients of the construction of the C^* -algebra of a groupoid (introduced by Renault in [19]) and to collect some results on the independence of the C^* -algebra on the choice of Haar system.

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