

SOME COMMON FIXED POINT THEOREMS USING IMPLICIT RELATION IN 2-BANACH SPACES

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Abstract. In this article, we study the existence and uniqueness of a common fixed point of family of self mappings satisfying implicit relation on a 2-Banach space. We also prove well-posedness of a common fixed point problem.

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2010 Mathematics Subject Classification: 47H10; 54H25.

Keywords: common fixed point; asymptotically T-regular; well-posedness; 2-Banach space.

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Surveys in Mathematics and its Applications **10** (2015), 159 – 168
<http://www.utgjiu.ro/math/sma>