

ABSTRACT. Let \mathcal{C} denote the category of Hilbert modules which are similar to contractive Hilbert modules. It is proved that if $H_0, H \in \mathcal{C}$ and if H_1 is similar to an isometric Hilbert module, then the sequence

$$0 \rightarrow H_0 \rightarrow H \rightarrow H_1 \rightarrow 0$$

splits. Thus the isometric Hilbert modules are projective in \mathcal{C} . It follows that $\text{Ext}_{\mathcal{C}}^n(K, H) = 0$, whenever $n > 1$, for $H, K \in \mathcal{C}$. In addition, it is proved that (Hilbert modules similar to) unitary Hilbert modules are projective in the category \mathcal{H} of all Hilbert modules. Connections with the conjecture that \mathcal{C} is a *proper* subset of \mathcal{H} are discussed.