

ABSTRACT. One considers the class of maps $u : D \rightarrow S^2$, which map ∂D to one point in S^2 . If u were also harmonic, then it is known that u must be constant. However, if u is instead f -harmonic — a critical point of the energy functional

$$\frac{1}{2} \int_D f(x) |\nabla u(x)|^2$$

— then this need not be true. We shall see that there exist functions $f : D \rightarrow (0, \infty)$ and nonconstant f -harmonic maps $u : D \rightarrow S^2$ which map the boundary to one point. We will also see that there exist nonconstant f for which, there is no nonconstant f -harmonic map in this class. Finally, we see that there exists a nonconstant f -harmonic map from the torus to the 2-sphere.