

ABSTRACT. Let  $F$  be an algebraically closed field of characteristic 0 and  $f(x)$  a polynomial of degree strictly greater than one in  $F[x]$ . We show that the number of degree  $k$  polynomials with coefficients in  $F$  that commute with  $f$  (under composition) is either zero or equal to the number of degree one polynomials with coefficients in  $F$  that commute with  $f$ . As a corollary, we obtain a theorem of E. A. Bertram characterizing those polynomials commuting with a Chebyshev polynomial.