A Reliable Multicast Framework for Light-weight Sessions and Application Level Framing

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ABSTRACT

This paper[1] describes SRM (Scalable Reliable Multicast), a reliable multicast framework for application level framing and light-weight sessions. The algorithms of this framework are efficient, robust, and scale well to both very large networks and very large sessions. The framework has been prototyped in wb, a distributed whiteboard application, and has been extensively tested on a global scale with sessions ranging from a few to more than 1000 participants. The paper describes the principles that have guided our design, including the IP multicast group delivery model, an end-to-end, receiver-based model of reliability, and the application level framing protocol model. As with unicast communications, the performance of a reliable multicast delivery algorithm depends on the underlying topology and operational environment. We investigate that dependence via analysis and simulation, and demonstrate an adaptive algorithm that uses the results of previous loss recovery events to adapt the control parameters used for future loss recovery. With the adaptive algorithm, our reliable multicast delivery algorithm provides good performance over a wide range of underlying topologies.

1 Introduction

Several researchers have proposed generic reliable multicast protocols, much as TCP is a generic transport protocol for reliable unicast transmission. In this paper we take a different view: unlike the unicast case where requirements for reliable, sequenced data delivery are fairly general, different multicast applications have widely different requirements for reliability. For example, some applications require that delivery obey a total ordering while many others do not. Some applications have many or all the members sending data while others have only one data source. Some applications have replicated data, for example in an n-redundant file store, so several members are capable of transmitting a data item while for others all data originates at a single source. These differences all affect the design of a reliable multicast protocol. Although one could design a protocol for the worst-case requirements, e.g., guarantee totally ordered delivery of replicated data from a large number of sources, such an approach results in substantial overhead for applications with more modest requirements. One cannot make a single reliable multicast delivery scheme that simultaneously meets the functionality, scalability and efficiency requirements of all applications.

The weakness of "one size fits all" protocols has long been recognized. In 1990 Clark and Tennenhouse proposed a new protocol model called Application Level Framing (ALF) which explicitly includes an application's semantics in the design of that application's protocol [CT90]. ALF was later elaborated with a light-weight rendezvous mechanism based on the IP multicast distribution model, and with a notion of receiver-based adaptation for unreliable, real-time applications such as audio and video conferencing. The result, known as Light-Weight Sessions (LWS), has been very successful in the design of wide-area, large-scale, conferencing applications. This paper further evolves the principles of ALF and LWS to add a framework for scalable reliable multicast (SRM).

ALF says that the best way to meet diverse application requirements is to leave as much functionality and flexibility

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[1] An earlier version of this paper appeared in ACM SIGCOMM 95. This version corrects errors in the graphs of that earlier version.

as possible to the application. Therefore our algorithms are designed to meet only the minimal definition of reliable multicast, i.e., eventual delivery of all the data to all the group members, without enforcing any particular delivery order. We believe that if the need arises, machinery to enforce a particular delivery order can be easily added on top of this reliable delivery service.

The design is also heavily based on the group delivery model that is the centerpiece of the IP multicast protocol [D91]. In IP multicast, data sources simply send to the group's multicast address (a normal IP address chosen from a reserved range of addresses) without needing any advance knowledge of the group membership. To receive any data sent to the group, receivers simply announce that they are interested (via a "join" message broadcast on the local subnet) — no knowledge of the group membership or active senders is required. Each receiver joins and leaves the group individually, without affecting the data transmission to any other member. Our multicast delivery framework further enhances the multicast group concept by maximizing information and data sharing among all the members, and strengthens the individuality of membership by making each member responsible for its own correct reception of all the data.

Finally, our design attempts to follow the core design principles of TCP/IP. First, we require only the basic IP delivery model — best-effort with possible duplication and reordering of packets — and build the reliability on an end-to-end basis. No change or special support is required from the underlying IP network. Second, in a fashion similar to TCP adaptively setting timers or congestion control windows, our algorithms dynamically adjust their control parameters based on the observed performance within a session. This allows applications using this model to adapt to a wide range of group sizes, topologies and link bandwidths while maintaining robust and high performance.

The paper proceeds as follows: Section 2 discusses general issues for reliable multicast delivery. Section 3 describes in detail the reliable multicast algorithm embedded in the wb implementation. Section 4 discusses the performance of the algorithm in simple topologies such as chains, stars, and bounded-degree trees, and Section 5 presents simulation results from more complex topologies. Section 6 discusses extensions to the basic scheme embedded in wb, such as adaptive algorithms for adjusting the timer parameters and algorithms for local recovery. Section 7 discusses both the application-specific aspects of wb's reliable multicast algorithms as well as the aspects of the underlying approach that have general applicability. Section 8 discusses related work on reliable multicast. Section 9 discusses future work on the congestion control algorithms. Finally, Section 10 presents conclusions.

2 The design of reliable multicast

2.1 Reliable data delivery: adding the word "multicast"

The problem of reliable (unicast) data delivery is well understood and a variety of well-tested solutions are available. However, adding the word 'multicast' to the problem statement significantly changes the solution set. For example, in any reliable protocol some party must take responsibility for loss detection and recovery. Because of the "fate-sharing" implicit in unicast communication, i.e., the data transmission fails if either of the two ends fails, either the sender or receiver can take on this role. In TCP, the sender times transmissions and keeps retransmitting until an acknowledgment is received. NETBLT [CLZ87] uses the opposite model and makes the receiver responsible for all loss detection and recovery. Both approaches have been shown to work well for unicast.

However, if a TCP-style, sender-based approach is applied to multicast distribution, a number of problems occur. First, because data packets trigger acknowledgments (positive or negative) from all the receivers, the sender is subject to the well-known ACK implosion effect. Also, if the sender is responsible for reliable delivery, it must continuously track the changing set of active receivers and the reception state of each. Since the IP multicast model deliberately imposes a level of indirection between senders and receivers (i.e., data is sent to the multicast group, not to the set of receivers), the receiver set may be expensive or impossible to obtain. Finally, the algorithms that are used to adapt to changing network conditions tend to lose their meaning in the case of multicast. E.g., how should the round-trip time estimate for a retransmit timer be computed when there may be several orders of magnitude difference in propagation time to different receivers? What is a congestion window if the delay-bandwidth product to different receivers varies by orders of magnitude? What self-clocking information exists in the ACK stream(s) if some receivers share one bottleneck link and some another?

These problems illustrate that single-point, sender-based control does not adapt or scale well for multicast delivery. Since members of a multicast group have different communication paths and may come and go at any time, the "fate-shared" coupling of sender and receiver doesn't generalize to multicast. None of the problems described above exist with NETBLT-style, receiver-based reliability (e.g., since each receiver keeps its own reception state, the per-host state burden is constant, independent of group size, and the fact that group membership can't be known is irrelevant). Thus it is clear that receiver-based reliability is a far better building block for reliable multicast [PTK94].

Another unicast convention that migrates poorly to multicast has to do with the vocabulary used by the sender and receiver(s) to describe the progress of their communication. A receiver can request a retransmission either in application data units ("sector 5 of file sigcomm-slides.ps") or in terms

of the shared communication state ("sequence numbers 2560 to 3071 of this conversation"). Both models have been used successfully (e.g., NFS uses the former and TCP the latter) but, because the use of communication state for naming data allows the protocol to be entirely independent of any application's namespace, it is by far the most popular approach for unicast applications. However, since the multicast case tends to have much weaker and more diverse state synchronization, using that state to name data works badly. E.g., if a receiver joins a conversation late and receives sequence numbers 2560 to 3071, it has no idea of what's been missed (since the sender's starting number is arbitrary) and so can neither do anything useful with the data nor make an intelligent request for retransmission. If receivers hear from a sender again after a lengthy network partition, they have no way of knowing whether "2560" is a retransmission of data they received before the partition or is completely new (due to sequence number wrapping during the partition). Thus the "naming in application data units (ADUs)" model works far better for multicast. Use of this model also has two beneficial side effects. As [CT90] points out, a separate protocol namespace can impose delays and inefficiencies on an application, e.g., TCP will only deliver data in sequence even though a file transfer application might be perfectly happy to receive sectors in any order. The ADU model eliminates this delay and puts the application back in control. Also, since ADU names can be made independent of the sending host, it is possible to use the anonymity of IP multicast to exploit the redundancy of multiple receivers. E.g., if some receiver asks for a retransmit of "sigcomm-slides.ps sector 5", any member who has a copy of the data, not just the original sender, can carry out the retransmission.

2.2 Reliable multicast requirements

While the ALF model says that applications should be actively involved in their communications and that communication should be done in terms of ADUs rather than some generic protocol namespace, we do not claim that every application's protocol must be completely different from every other's or that there can be no shared design or code. A great deal of design commonality is imposed simply because different applications are attempting to solve the same problem: scalable, reliable, multipoint communication over the Internet. As Section 2.1 pointed out, just going from unicast to multicast greatly limits the viable protocol design choices. In addition, experience with the Internet has shown that successful protocols must accommodate many orders of magnitude variation in every possible dimension. While several algorithms meet the constraints of Section 2.1, very few of them continue to work if the delay, bandwidth and user population are all varied by factors of 1000 or more.

In the end we believe the ALF model results in a skeleton or template which is then fleshed out with application specific details. Portions of that skeleton are completely determined by network dynamics and scaling considerations and apply to any application. So, for example, the scalable request and repair algorithms described in Sections 3 through 6 are completely generic and apply to a wide variety of reliable multicast applications. Each different application supplies this reliability framework with a namespace to talk about what data has been sent and received; a policy and machinery to determine how bandwidth should be apportioned between a participant in the group, the group as a whole, and other users of the net; and a local send policy that a participant uses to arbitrate the different demands on its bandwidth (e.g., locally originated data, repair requests and responses, etc.). It is the intent of this paper to describe the skeleton common to scalable, reliable multicast applications. However, to make the ideas concrete, we first describe a complete, widely used application — wb, the LBL network whiteboard — that has been implemented according to this model. After mentioning some details of its operation that are direct implications of the design considerations in Section 2.1, we then factor out the wb specifics to expose the generic, scalable, reliable multicast skeleton underneath. The remaining sections of this paper are an exploration of that skeleton.

2.3 The wb framework

Wb is a network conferencing tool designed and implemented by McCanne and Jacobson [J92, J94a, M92] that provides a distributed whiteboard. The whiteboard separates the drawing into pages, where a new page can correspond to a new viewgraph in a talk or the clearing of the screen by a member of a meeting. Any member can create a page and any member can draw on any page.[2] Each member is identified by a globally unique identifier, the Source-ID, and each page is identified by the Source-ID of the initiator of the page and a page number locally unique to that initiator. Each member drawing on the whiteboard produces a stream of drawing operations that are timestamped and assigned sequence numbers, relative to the sender. Most drawing operations are idempotent and are rendered immediately upon receipt. Each member's graphics stream is independent from that of other sites.

The following assumptions are made in wb's reliable multicast design:

- All data has a unique name.

[2] There are floor control mechanisms, largely external to wb, that can be used if necessary to control who can create or draw on pages. These can be combined with normal Internet privacy mechanisms (e.g., symmetric-key encryption of all the wb data) to limit participation to a particular group and/or with normal authentication mechanisms (e.g., participants signing their drawing operations via public-key encryption of a cryptographic hash of the drawop). The privacy, authentication and control mechanisms are completely orthogonal to the reliability machinery that is the subject of this paper and will not be described here. For further details see [MJ95, J94].

This global name consists of the end host's Source-ID and a locally unique sequence number.

- The name always refers to the same data.

  It is impossible to achieve consistency among different receivers in the face of late arrivals and network partitions if, say, drawop "floyd:5" initially means a blue line and later turns into a red circle. This does not mean that the drawing can't change, only that drawops must effect the change. E.g., to change a blue line to a red circle, a "delete" drawop for "floyd:5" is sent, then a drawop for the circle is sent.

- Source-ID's are persistent.

  A user will often quit a session and later re-join, obtaining the session's history from the network. By ensuring that Source-ID's are persistent across invocations of the application, the user maintains ownership of any data created before quitting.

- IP multicast datagram delivery is available.

- All participants join the same multicast group; there is no distinction between senders and receivers.

Wb has no requirement for ordered delivery because most operations are idempotent. Operations that are not strictly idempotent, such as a "delete" that references an earlier drawop, can be patched after the fact, when the missing data arrives. A receiver uses the timestamps on the drawing operations to determine the rendering order. This coarse synchronization mechanism captures the temporal causality of drawing operations at a level appropriate for the application, without the added complexity and delay of protocols that provide guaranteed causal ordering.

3 Wb's instantiation of the reliable multicast algorithm

Whenever new data is generated by wb, it is multicast to the group. Each member of the group is individually responsible for detecting loss and requesting retransmission. Loss is normally detected by finding a gap in the sequence space. However, since it is possible that the last drawop of a set is dropped, each member sends low-rate, periodic, session messages that announce the highest sequence number received from every member that has written on the page currently being displayed. In addition to the reception state, the session messages contain timestamps that are used to estimate the distance (in time) from each member to every other (described in Section 3.1).

When receiver(s) detect missing data, they wait for a random time determined by their distance from the original source of the data, then send a repair request (the timer calculations are described in detail in Section 3.2). As with the original data, repair requests and retransmissions are always multicast to the whole group. Thus, although a number of hosts may all miss the same packet, a host close to the point of failure is likely to timeout first and multicast the request. Other hosts that are also missing the data hear that request and suppress their own request. (This prevents a request implosion.) Any host that has a copy of the requested data can answer a request. It will set a repair timer to a random value depending on its distance from the sender of the request message and multicast the repair when the timer goes off. Other hosts that had the data and scheduled repairs will cancel their repair timers when they hear the multicast from the first host. (This prevents a response implosion). In a topology with diverse transmission delays, a lost packet is likely to trigger only a single request from a host just downstream of the point of failure and a single repair from a host just upstream of the point of failure.

3.1 Session messages

As mentioned above, each member sends periodic session messages that report the sequence number state for active sources. Receivers use these session messages to determine the current participants of the session and to detect losses. The average bandwidth consumed by session messages is limited to a small fraction (e.g., 5%) of the session data bandwidth using the algorithm developed for vat and described in [SCFJ94].

In a large, long-lived session, the state would become unmanageable if each receiver had to report the sequence numbers of everyone who had ever written to the whiteboard. The "pages" mentioned above are used to partition the state and prevent this explosion. Each member only reports the state of the page it is currently viewing. If a receiver joins late, it may issue *page requests* to learn the existence of pages and the sequence number state in each page. We omit the details of the page state recovery protocol as it is almost identical to the repair request / response protocol for data.

In addition to state exchange, receivers use the session messages to estimate the one-way distance between nodes. All whiteboard packets, including session packets, include a Source-ID and a timestamp. The session packet timestamps are used to estimate the host-to-host distances needed by the repair algorithm.

The timestamps are used in a highly simplified version of the NTP time synchronization algorithm [M84]. Assume that host A sends a session packet P_1 at time t_1 and host B receives P_1 at time t_2. At some later time, t_3, host B generates a session packet P_2, marked with (t_1, Δ) where $\Delta = t_3 - t_2$ (time t_1 is included in P_2 to make the algorithm robust to lost session packets). Upon receiving P_2 at time t_4, host A can estimate the latency from host B to host A as $(t_4 - t_1 - \Delta)/2$. Note that while this estimate does assume that the paths are symmetric, it does not assume synchronized clocks.

3.2 Loss recovery

The loss recovery algorithm provides the foundation for reliable delivery. In this section we describe the loss recovery algorithm originally designed for wb; Section 6.1 describes a modified version of this algorithm with an adaptive adjustment of the timer parameters.

When host A detects a loss, it schedules a repair request for a random time in the future. The request timer is chosen from the uniform distribution on $[C_1 d_{S,A}, (C_1+C_2) d_{S,A}]$ seconds, where $d_{S,A}$ is host A's estimate of the one-way delay to the original source S of the missing data. When the request timer expires, host A sends a request for the missing data, and doubles the request timer to wait for the repair.

If host A receives a request for the missing data before its own request timer for that data expires, then host A does a (random) exponential backoff, and resets its request timer. That is, if the current timer had been chosen from the uniform distribution on

$$2^i[C_1 d_{S,A}, (C_1 + C_2) d_{S,A}],$$

then the backed-off timer is randomly chosen from the uniform distribution on

$$2^{i+1}[C_1 d_{S,A}, (C_1 + C_2) d_{S,A}].$$

When host B receives a request from A that host B is capable of answering, host B sets a repair timer to a value from the uniform distribution on

$$[D_1 d_{A,B}, (D_1 + D_2) d_{A,B}]$$

seconds, where $d_{A,B}$ is host B's estimate of the one-way delay to host A. If host B receives a repair for the missing data before its repair timer expires, then host B cancels its repair timer. If host B's repair timer expires before it receives a repair, then host B multicasts the repair. Because host B is not responsible for host A's reliable data reception, it does not verify whether host A actually receives the repair.

Due to the probabilistic nature of these algorithms, it is not unusual for a dropped packet to be followed by more than one request. Thus, a host could receive a duplicate request immediately after sending a repair, or immediately after receiving a repair in response to its own earlier request. In order to prevent duplicate requests from triggering a responding set of duplicate repairs, host B ignores requests for data D for $3\,d_{S,B}$ seconds after sending or receiving a repair for that data, where host S is either the original source of data D or the source of the first request.

Because data represents idempotent operations, loss recovery can proceed independently from the transmission of new data. Similarly, recovery for losses from two different sources can also proceed independently. Since transmission bandwidth is often limited, a single transmission rate is allocated to control the throughput across all these different modes of operation, while the application determines the order of packet transmission according to their relative importance. In wb, the highest priority packets are repairs for the current page, middle priority are new data, and lowest priority are repairs for previous pages.

3.3 Bandwidth limitations

The congestion control mechanism for whiteboard sessions is based on a (fixed, in current implementations) maximum bandwidth allocation for each session. Each wb session has a sender bandwidth limit advertised as part of the sd announcement. A typical value is 64 Kbps; in this case a wb session costs no more (and typically considerably less) than the accompanying audio session. Individual members use a token bucket rate limiter to enforce this peak rate on transmissions. This peak rate is mostly relevant when a source distributes a postscript file for a new page of the whiteboard, or when a late arrival requests the past history of the whiteboard session.

3.4 Recovery from partitioning

The whiteboard does not require special mechanisms for the detection or recovery from network partitioning. Because wb relies on the underlying concept of an IP multicast group, where members can arrive and depart independently, wb does not distinguish a partitioning from a normal departure of members from the wb session.

During a partition of a session, users can simply continue using the whiteboard in the connected components of the partitions. Because pages are identified by the Source-ID of the initiator of the page, along with the page number for that initiator, members can continue creating new pages during the partition (e.g., "Floyd:3" in one half of the partition, and "Zhang:5" in the other). After recovery each page will still have a unique page ID and the repair mechanism will distribute any new state throughout the entire group.

Almost all of the design described in this section is present in version 1.59 of wb; some omissions are pending implementation. These omissions include the measurements of one-way delays and the rate-limiting mechanisms.

4 Request/repair algorithms for simple topologies

Building on our initial design experiences in wb, we turn to a more general investigation of the request/repair algorithms. The algorithms described in the remainder of the paper have been implemented only within our simulation framework.

Given that multiple hosts may detect the same losses, and multiple hosts may attempt to handle the same repair request, the goal of the request/repair timer algorithms is to de-synchronize host actions to keep the number of duplicates low. Among hosts that have diverse delays to other hosts in the same group, this difference in delay can be used to differentiate hosts; for hosts that have similar delays to reach

others, we can only rely on randomization to de-synchronize their actions.

This section discusses a few simple, yet representative, topologies, namely chain, star, and tree topologies, to provide a foundation for understanding the request/repair algorithms in more complex environments. For a chain the essential feature of a request/repair algorithm is that the timer value be a function of distance. For a star topology the essential feature of the request/repair algorithm is the randomization used to reduce implosion. Request/repair algorithms in a tree combine both the randomization and the setting of the timer as a function of distance. This section shows that the performance of the request/repair algorithms depends on the underlying network topology.

4.1 Chains

Figure 1 shows a chain topology where all nodes in the chain are members of the multicast session. Each node in the underlying multicast tree has degree at most two. The chain is an extreme topology where a simple deterministic request/repair algorithm suffices; in this section we assume that $C_1, D_1 = 1$, and that $C_2, D_2 = 0$.

For the chain, as in most of the other scenarios in this paper, link distance and delay are both normalized. We assume that packets take one unit of time to travel each link, i.e. all links have distance of 1.

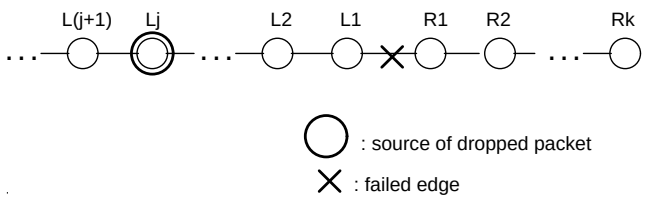


Figure 1: A chain topology.

In Figure 1 the nodes in the chain are labeled as either to the right or to the left of the congested link. Assume that source L_j multicasts a packet that is subsequently dropped on link (L_1, R_1), and that the second packet sent from source L_j is not dropped. We call the edge that dropped the packet, whether due to congestion or to other problems, the *congested* link. Assume that the right-hand nodes each detect the failure when they receive the second packet from L_j.

Assume that node R_1 first detects the loss at time t, and that each link has distance 1. Then node R_1 multicasts a request at time $t + j$. Node L_1 receives the request at time $t + j + 1$ and multicasts a repair at time $t + j + 2$. Node R_k receives the repair at time $t + k + j + 2$.

Note that all nodes to the right of node R_1 receive the request from R_1 before their own request timers expire. We call this *deterministic suppression*. We leave it as an exercise for the reader to verify that, due to deterministic suppression, there will be only one request and one repair.

Had the loss repair been done by unicast, i.e. node R_k sent a unicast request to the source L_j as soon as it detected the failure and L_j sent a unicast repair to R_k as soon as it received the request, node R_k would not receive the repair until time $t + 2j + 3k$. Thus, with a chain and with a simple deterministic request/repair algorithm, the furthest node receives the repair sooner than it would if it had to rely on its own unicast communication with the original source. While the original source and the intended recipient of the dropped packet could be arbitrarily far from the congested link, in the multicast repair algorithm both the request and the repair come from the node immediately adjacent to the congested link.

4.2 Stars

For the star topology in Figure 2 we assume that all links are identical and that the center node is not a member of the multicast group. For a star topology, setting the request timer as a function of the distance from the source is not an essential feature, as all nodes detect a loss at exactly the same time. Instead, the essential feature of the request/repair algorithm in a star is the randomization used to reduce implosion; we call this *probabilistic suppression*.

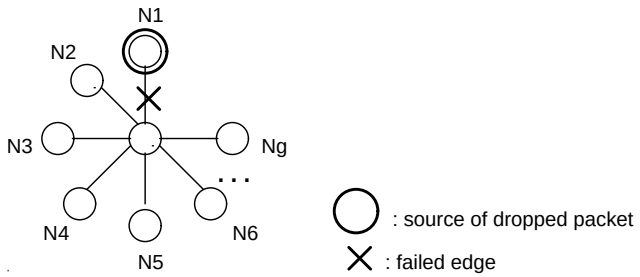


Figure 2: A star topology.

For the star topology in Figure 2 assume that the first packet from node N_1 is dropped on the adjacent link. There are G members of the multicast session, and the other members detect the loss at exactly the same time. For the discussion of this topology we assume that $C_1, D_1 = 0$; because all nodes detect losses and receive requests at the same time, C_1 and D_1 are not needed to amplify differences in delay. The only benefit in setting C_1 greater than 0 is to avoid unnecessary requests from out-of-order packets.

If C_2 is at most 1, then there will always be $G - 1$ requests. Increasing C_2 reduces the expected number of requests but increases the expected time until the first request is sent. For $C_2 > 1$, the expected number of requests is roughly $1 + (G - 2)/C_2$, and the expected delay until the first timer expires is $2C_2/G$ seconds (where one unit of time is one second).[3] For example, if C_2 is set to $\sqrt{G}$, then the expected

[3]The $G - 1$ nodes all detect the failure at the same time, and all set their timers to a uniform value in an interval of width $2C_2$. If the first timer

number of requests is roughly $\sqrt{G}$, and the expected delay until the first timer expires is $2/\sqrt{G}$ seconds. The same remarks apply to D_2 with respect to repairs.

4.3 Bounded-degree trees

The request/repair performance in a tree topology uses both the deterministic suppression described for chain topologies and the probabilistic suppression described for star topologies. Consider a network topology of a bounded-degree tree with N nodes where interior nodes have degree p. A tree topology combines aspects of both chains and stars. The timer value should be a function of distance, to enable requests and repairs to suppress request and repair timers at nodes further down in the tree. In addition, randomization is needed to reduce request/repair implosion from nodes that are at an equal distance from the source (of the dropped packet, or of the first request).

We assume that node S in the tree is the source of the dropped packet, and that link (B,A) drops a packet from source S. We call nodes on the source's side of the congested link (including node B) *good* nodes, and we call nodes on the other side of the congested link (including node A) *bad* nodes. Node A detects the dropped packet at time t, when it receives the next packet from node S. We designate node A as a *level-0* node, and we call a bad node a *level-i* node if it is at distance i from node A.

Assume that the source of the dropped packet is at distance j from node A. Node A's request timer expires at time

$$t + C_1 j + U_1[C_2]j,$$

where $U[C_2]$ denotes a uniform random variable between 0 and C_2. Assuming that node A's request is not suppressed, a level-i node receives node A's request at time

$$t + i + C_1 j + U_1[C_2]j.$$

Node B receives node A's repair request at time

$$t + 1 + C_1 j + U_1[C_2]j.$$

A bad level-i node detects the loss at time $t + i$, and such a node's request timer expires at some time

$$t + i + C_1(i + j) + U_2[C_2](i + j).$$

Note that regardless of the values of $U_1[C_2]$ and $U_2[C_2]$, a level-i node receives node A's request by time $t + i + C_1 j + C_2 j$, and a level-i node's request timer expires no sooner than $t + i + C_1(i + j)$. If

$$t + i + C_1 j + C_2 j \leq t + i + C_1(i + j),$$

that is, if

$$\frac{C_2}{C_1} j \leq i,$$

then the level-i node's request timer will always be suppressed by the request from the level-0 node. Thus, the smaller the ratio C_2/C_1, the fewer the number of levels that could be involved in duplicate requests. This relation also demonstrates why the number of duplicate requests or repairs is smaller when the source (of the dropped packet, or of the request) is close to the congested link.

Note that the parameter C_1 serves two different functions. A smaller value for C_1 gives a smaller delay for node B to receive the first request. At the same time, for nodes further away from the congested link, a larger value for C_1 contributes to suppressing additional levels of request timers. A similar tradeoff occurs with the parameter C_2. A smaller value for C_2 gives a smaller delay for node B to receive the first repair request. At the same time, as illustrated with star topologies, a larger value for C_2 helps to prevent duplicate requests from session members at the same distance from the congested link. Similar remarks apply to the functions of D_1 and D_2 in the repair timer algorithm.

5 Simulations of the request and repair algorithms

For a given underlying network, set of session members, session sources, and congested link, it should be feasible to analyze the behavior of the repair and request algorithms, given fixed timer parameters C_1, C_2, D_1, and D_2. However, we are interested in the repair and request algorithms across a wide range of topologies and scenarios. We use simulations to examine the performance of the request/repair algorithms for individual packet drops in random and bounded-degree trees. We do not claim to be presenting realistic topologies or typical patterns of packet loss.

The simulations in this section show that the request/repair algorithms with fixed timer parameters perform well in a random or bounded-degree tree when every node in the underlying tree is a member of the multicast session. The request/repair algorithms perform somewhat less well for a sparse session, where the session size is small relative to the size of the underlying network. This motivates the development on the adaptive request/repair algorithm in Section 6.1, where the timer parameters C_1, C_2, D_1, and D_2 are adjusted in response to past performance.

In these simulations the fixed timer parameters are set as follows: $C_1, C_2 = 2$, and $D_1, D_2 = \log_{10} G$, where G is the number of members in the same multicast session. The choice of $\log_{10} G$ for D_1 and D_2 is not critical, but gives slightly better performance than $D_1, D_2 = 1$ for large G.

Each simulation constructs either a random tree or a bounded degree tree with N nodes as the network topology. Next, G of the N nodes are randomly chosen to be session

expires at time t, then the other $G - 2$ receivers receive that first request at time $t + 2$. So the expected number of duplicate requests is equal to the expected number of timers that expire in the interval $[t, t + 2]$.

members, and a source S is randomly chosen from the G session members.

We assume that messages are multicast to members of the multicast group along a shortest-path tree from the source of the message. In each simulation we randomly choose a link L on the shortest-path tree from source S to the G members of the multicast group. We assume that the first packet from source S is dropped by link L, and that receivers detect this loss when they receive the subsequent packet from source S.

5.1 Simulations on random trees

We first consider simulations on random labeled trees of N nodes, constructed according to the labeling algorithm in [Pa85, p.99]. These trees have unbounded degree, but for large N, the probability that a particular vertex in a random labeled tree has degree at most four approaches 0.98 [Pa85, p.114]. Figure 3 shows simulations of the request/repair algorithm for this case, where all N nodes in the tree are members of the multicast session (that is, $G = N$). For each graph the x-axis shows the session size G; twenty simulations were run for each value of G. Each simulation is represented by an jittered dot, and the median from the twenty simulations is shown by a solid line. The two dotted lines mark the upper and lower quartiles; thus, the results from half of the simulations lie between the two dotted lines.

The top two graphs in Figure 3 show the number of requests and repairs to recover from a single loss. The bottom graph shows the delay of the last node in the multicast session to receive the repair. For each member affected by the loss, we define the delay as the time from when the member first detected the loss until the member first received a repair. The graph shows this delay as a multiple of RTT, the roundtrip time from the receiver to the original source of the dropped packet.

Note that with unicast communications the ratio of delay to RTT is at least one. For a unicast receiver that detects a packet loss by waiting for a retransmit timer to time out, the typical ratio of delay to RTT is closer to 2. As the earlier discussion of chain topologies shows, with multicast request/repair algorithms the ratio of delay to RTT can sometimes be less than one, because the request and/or repair could each come from a node close to the point of failure.

Figure 3 shows that the repair/request algorithm works well for a tree topology where all nodes of the tree are members of the multicast session. There is usually only one request and one repair. (Some lack of symmetry results from the fact that the original source of the dropped packet might be far from the point of failure, while the first request comes from a node close to the point of failure.) The average recovery delay for the farthest node is roughly 2 RTT, competitive with the average delay available from a unicast algorithm such as TCP. The results are similar in simulations where the congested link is chosen adjacent to the source of the dropped packet, and for simulations on a bounded-degree tree of size $N = G$ where interior nodes have degree 4.

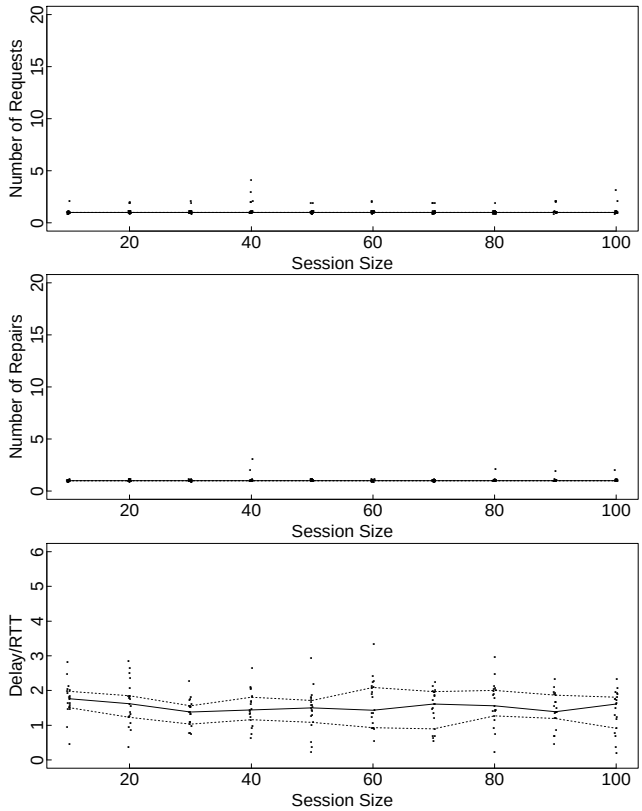


Figure 3: Random trees with a random congested link, where all nodes are members of the multicast session.

5.2 Simulations on large bounded-degree trees

The performance of the request/repair algorithms with fixed timer parameters is less optimal when the underlying network is a large bounded-degree tree. The underlying topology for the simulations in this section is a balanced bounded-degree tree of $N = 1000$ nodes, with interior nodes of degree four. In these simulations the session size G is significantly less than N. For a session that is sparse relative to the underlying network, the nodes close to the congested link might not be members of the session.

As Figure 4 shows, the average number of repairs for each loss is somewhat high. In simulations where the congested link is always adjacent to the source, the number of repairs is low but the average number of requests is high.

[FJLMZ95] shows the performance of the request/repair algorithm on a range of topologies. These include topologies where each of the N nodes in the underlying network is a router with an adjacent ethernet with 5 workstations, point-to-point topologies where the edges have a range of propagation delays, and topologies where the underlying network is more dense that a tree. None of these variations that we

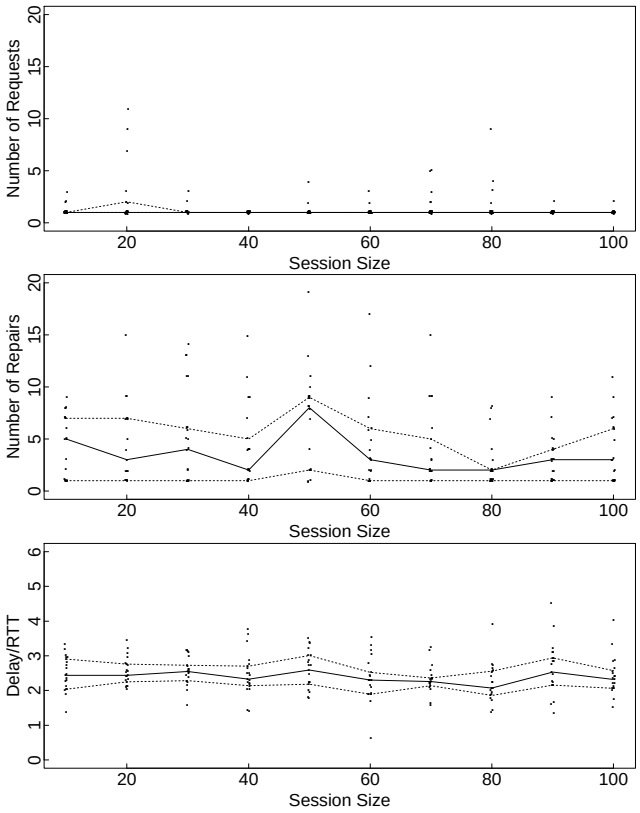


Figure 4: Bounded-degree tree, degree 4, 1000 nodes, with a random congested link.

have explored have significantly affected the performance of the request/repair algorithms with fixed timer parameters.

6 Extending the basic approach

6.1 Adaptive adjustment of random timer algorithms

The close connection of the loss recovery performance with the underlying topology of the network suggests that the timer parameters C_1, C_2, D_1, and D_2 be adjusted in response to the past behavior of the request/repair algorithms. In this section we describe an adaptive algorithm that adjusts the timer parameters as a function of both the delay and of the number of duplicate requests and repairs in recent loss recovery exchanges.

Figure 5 gives the outline of the dynamic adjustment algorithm for adjusting the timer parameter C_2, which controls the width of the request timer interval. If the average number of duplicate requests is too high, then the adaptive algorithm increases the request timer interval. Alternately, if the average number of duplicates is okay but the average delay in sending a request is too high, then the adaptive algorithm decreases the request timer interval. In this fashion the adaptive algorithm can adapt the timer parameters not only to fit the fixed underlying topology, but also to fit a changing session

```
Before each new request timer is set:
   if ave. dup.  requests high
      increase request timer interval
   else if ave. dup. requests low
   and ave. req. delay too high
      decrease request timer interval
```

Figure 5: Dynamic adjustment algorithm for request timer interval.

membership and pattern of congestion.

First we describe how a session member measures the average delay and number of duplicate requests in previous loss recovery rounds in which that member has been a participant. A *request period* begins when a member first detects a loss and sets a request timer, and ends only when that member begins a new request period. The variable *dup_req* keeps count of the number of duplicate requests received during one request period; these could be duplicates of the most recent request or of some previous request, but do not include requests for data for which that member never set a request timer. At the end of each request period, the member updates *ave_dup_req*, the average number of duplicate requests per request period, before resetting *dup_req* to zero. The average is computed as an exponential-weighted moving average,

$$ave_dup_req \leftarrow (1-\alpha)\, ave_dup_req + \alpha\, dup_req,$$

with $\alpha = 1/4$ in our simulations. Thus, *ave_dup_req* gives the average number of duplicate requests for those request events for which that member has actually set a request timer.

When a request timer either expires or is reset for the first time, indicating that either this member or some other member has sent a request for that data, the member computes req_delay, the delay from the time the request timer was first set (following the detection of a loss) until a request was sent (as indicated by the time that the request timer either expired or was reset). The variable req_delay expresses this delay as a multiple of the roundtrip time to the source of the missing data. The member computes the average request delay, ave_req_delay.

In a similar fashion, a *repair period* begins when a member receives a request and sets a repair timer, and ends when a new repair period begins. In computing *dup_rep*, the number of duplicate repairs, the member considers only those repairs for which that member at some point set a repair timer. At the end of a repair period the member updates *ave_dup_rep*, the average number of duplicate repairs.

When a repair timer either expires or is cleared, indicating that this member or some other member sent a repair for that data, the member computes rep_delay, the delay from the time the repair timer was set (following the receipt of a request) until a repair was sent (as indicated by the time that the repair timer either expired or was cleared). As above, the

variable rep_delay expresses this delay as a multiple of the roundtrip time to the source of the missing data. The member computes the average repair delay, ave_rep_delay.

```
After a request timer expires or is first
          reset:
   update ave_req_delay
Before each new request timer is set:
   update ave_dup_req
   if (ave_dup_req > AveDups))
      C1+ = 0.1
      C2+ = 0.5
   else if (ave_dup_req < AveDups−ε)
      if (ave_req_delay > AveDelay)
         C2− = 0.1
      if (ave_dup_req < 1/4)
         C1− = 0.05
   else C1+ = 0.05
```

Figure 6: Dynamic adjustment algorithm for request timer parameters. In our simulations $\epsilon = 0.1$

Figure 6 gives the adaptive adjustment algorithm used in our simulator to adjust the request timer parameters C_1 and C_2. The adaptive algorithm is based on comparing the measurements *ave_dup_req* and *ave_req_delay* with AveDups and AveDelay, the target bounds for the average number of duplicates and the average delay. An identical adjustment algorithm is used to adapt the repair timer parameters D_1 and D_2, based on the measurements *ave_dup_rep* and *ave_rep_delay*. Figure 7 gives the initial values used in our simulations for the timer parameters. All four timer parameters are constrained to stay within the minimum and maximum values in Figure 7.

```
Initial values:
   C1 = 2
   D1 = log10G
   C2 = 2
   D2 = log10G
Fixed parameters:
   MinC1 = 0.5;  MaxC1 = 2
   MinC2 = 1;  MaxC2 = G
   MinD1 = 0.5;  MaxD1 = log10G
   MinD2 = 1;  MaxD2 = G
   AveDups = 1
   AveDelay = 1
```

Figure 7: Parameters for adaptive algorithms

We are not trying to devise an optimal adaptive algorithm for reducing some function of both delay and of the number of duplicates; such an optimal algorithm could involve rather complex decisions about whether to adjust mainly C_1 or C_2, possibly depending on such factors as that member's relative distance to the source of the lost packet. Recall that increasing C_2 is guaranteed to reduce the number of duplicate requests; in contrast, increasing C_1 reduces the number of duplicate requests only when the members of the multicast group have diverse delays to reach each other. Our adaptive algorithm relies largely on adjustments of C_2 to reduce duplicates. Our adaptive algorithm only decreases C_1 when the average number of duplicates is already quite small (e.g., in scenarios where there are only one or two nodes capable of sending a request).

Because of the probabilistic nature of the repair and request algorithms, the behavior might vary over a fairly wide range even with a fixed set of timer parameters. Thus, the adaptive algorithm does not assume that the average number of duplicates is controlled until *ave_dup_req* is less than AveDups$-\epsilon$.

The numerical parameters in Figure 6 of 0.05, 0.1, and 0.5 were chosen somewhat arbitrarily. The adjustments of ± 0.05 and $+0.1$ for C_1 are intended to be small, as the adjustment of C_1 is not the primary mechanism for controlling the number of duplicates. The adjustments of -0.1 and $+0.5$ for C_2 are intended to be sufficiently small to minimize oscillations in the setting of the timer parameters. Sample trajectories of the request/repair algorithms confirm that the variations from the random component of the timer algorithms dominate the behavior of the algorithms, minimizing the effect of oscillations.

In our simulations we use a multiplicative factor of 3 rather than 2 for the request timer backoff described in Section 3.2. With a multiplicative factor of 2, and with an adaptive algorithm with small minimum values for C_1 and C_2, a single node that experiences a packet loss could have its request timer expire before receiving the repair packet, resulting in an unnecessary duplicate request.

Figures 8 and 9 show simulations comparing adaptive and non-adaptive algorithms. The simulation set in Figure 8 uses fixed values for the timer parameters, and the one in Figure 9 uses the adaptive algorithm. From the simulation set in Figure 4, we chose a network topology, session membership, and drop scenario that resulted in a large number of duplicate requests with the non-adaptive algorithm. The network topology is a bounded-degree tree of 1000 nodes with degree 4 for interior nodes, and the multicast session consists of 50 members.

Each of the two figures shows ten runs of the simulation, with 100 loss recovery rounds in each run. For each round of a simulation, the same topology and loss scenario is used, but a new seed is used for the pseudo-random number generator to control the timer choices for the requests and repairs. In each round a packet from the source is dropped on the congested link, a second packet from the source is not dropped, and the request/repair algorithms are run until all members

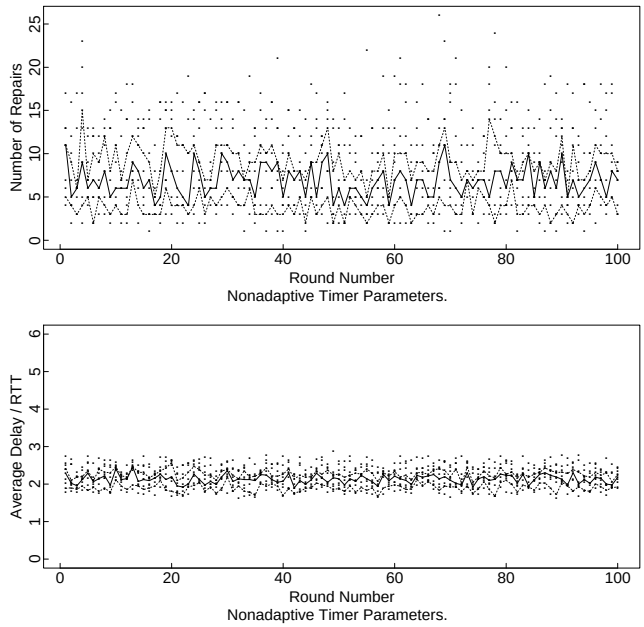


Figure 8: The non-adaptive algorithm.

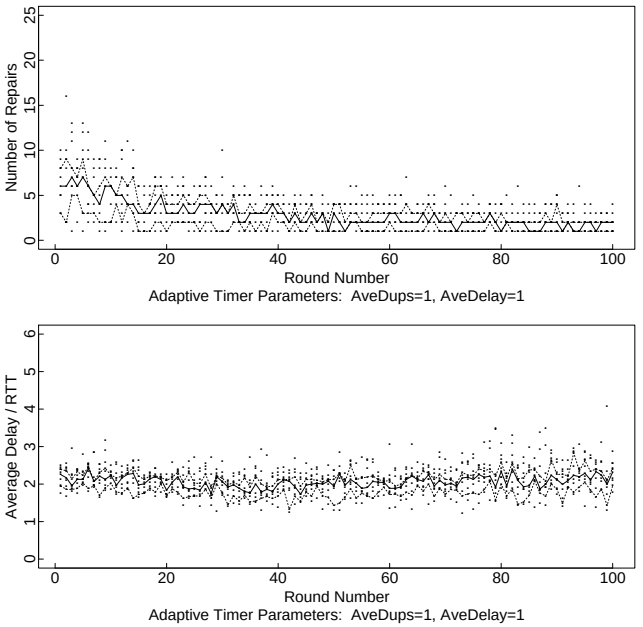
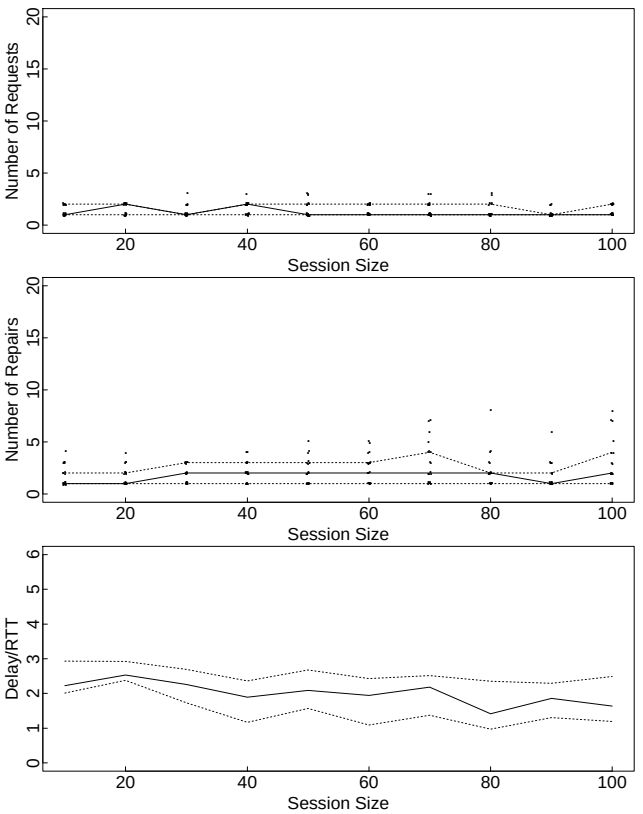


Figure 9: The adaptive algorithm.

have received the dropped packet. Each round of each simulation is marked with a dot, and a solid line shows the median from the ten simulations. The dotted lines show the upper and lower quartiles.

For the simulations in Figure 8 with fixed timer parameters, one round differs from another only in that each round uses a different set of random numbers for choosing the timers.

For the simulations with the adaptive algorithm in Figure 9, after each round of the simulation each session member uses the adaptive algorithms to adjust the timer parameters, based on the results from previous rounds. Figure 9 shows that for this scenario, the adaptive algorithms quickly reduce the average number of repairs with little penalty in additional delay. The average delay is roughly the same for the adaptive and the non-adaptive algorithms, but with the adaptive algorithm the delay has a somewhat higher variance.

Figure 10 shows the results of the adaptive algorithm on the same set of scenarios as that in Figure 4. For each scenario (i.e., network topology, session membership, source member, and congested link) in Figure 10, the adaptive algorithm is run repeatedly for 40 loss recovery rounds, and Figure 10 shows the results from the 40th loss recovery round. Comparing Figures 4 and 10 shows that the adaptive algorithm is effective in controlling the number of duplicates over a range of scenarios.

Simulations in [FJLMZ95] show that the adaptive algorithm works well in a wide range of conditions. These include scenarios where only one session member experiences the packet loss; where the congested link is chosen adjacent to the source of the packet to be dropped; and for a range of underlying topologies, including 5000-node trees, trees with