

# Package ‘npfseir’

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**Title** Nested Particle Filter for Stochastic SEIR Epidemic Models

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**Description** Implements the online Bayesian inference framework for joint state and parameter estimation in a stochastic Susceptible-Exposed-Infectious-Recovered (SEIR) epidemic model with a time-varying transmission rate. The log-transmission rate is modelled as a latent Ornstein-Uhlenbeck (OU) process with exact Gaussian discrete-time transitions. Inference is performed via the nested particle filter (NPF) of Crisan and Miguez (2018) <[doi:10.3150/17-BEJ954](https://doi.org/10.3150/17-BEJ954)>, which maintains an outer particle layer over the OU hyperparameters and, for each outer particle, an inner bootstrap filter over epidemic states. The Cori-style renewal-equation estimator follows Cori et al. (2013) <[doi:10.1093/aje/kwt133](https://doi.org/10.1093/aje/kwt133)>. The package also provides utilities for simulation, posterior summarisation, and forecasting.

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## Contents

npfseir-package . . . . .	2
---------------------------	---

cori_rt . . . . .	3
npf_seir . . . . .	4
ou_params . . . . .	6
plot.npf_seir . . . . .	6
predict.npf_seir . . . . .	7
print.npf_seir . . . . .	8
seir_simulate . . . . .	8
summary.npf_seir . . . . .	9

<b>Index</b>	<b>11</b>
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npfseir-package	<i>npfseir: Nested Particle Filter for Stochastic SEIR Epidemic Models</i>
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## Description

Implements the online Bayesian inference framework for stochastic SEIR epidemic models with latent Ornstein-Uhlenbeck transmission dynamics, as described in Feng and Wang (2025).

## Main functions

`npf_seir` Run the nested particle filter.  
`seir_simulate` Simulate a stochastic SEIR trajectory.  
`cori_rt` Cori-style renewal  $R_t$  estimator (illustrative).  
`ou_params` Exact OU discrete-time transition parameters.

## S3 methods for npf\_seir objects

`print`, `summary`, `plot`, `predict`.

## Author(s)

**Maintainer:** Weinan Wang <ww@ou.edu>

## References

Feng, W. and Wang, W. (2025). "Bayesian sequential inference for a stochastic SEIR model with latent transmission dynamics." *Preprint*.

Crisan, D. and Miguez, J. (2018). "Nested particle filters for online parameter estimation in discrete-time state-space Markov models." *Bernoulli*, 24(4B):3039–3086. doi:10.3150/17BEJ954

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cori_rt	<i>Cori-style renewal-equation <math>R_t</math> estimator</i>
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### Description

An in-house implementation of the sliding-window renewal-equation  $R_t$  estimator following Cori et al. (2013).

### Usage

```
cori_rt(
  incidence,
  tau = 7L,
  si_mean = 5.5,
  si_sd = 2.5,
  prior_a = 1,
  prior_b = 5
)
```

### Arguments

incidence	Numeric vector of length $T$ . Daily case counts.
tau	Integer. Sliding window length (days). Default 7.
si_mean	Positive numeric. Serial interval mean (days). Default 5.5.
si_sd	Positive numeric. Serial interval SD (days). Default 2.5.
prior_a	Positive numeric. Gamma prior shape on $R_t$ . Default 1.
prior_b	Positive numeric. Gamma prior scale on $R_t$ . Default 5.

### Details

**Important:** This is *not* a call to the R **EpiEstim** package and numerical agreement with that package has not been independently verified. It is provided for *illustrative comparison of estimands* only: the renewal-equation  $R_t$  and the compartmental  $R_t$  target different quantities once susceptible depletion is non-negligible (see Section 6.2 of Feng and Wang 2025).

The estimator uses gamma-conjugate updating over a  $\tau$ -day sliding window. The posterior is

$$R_t \mid \text{data} \sim \text{Gamma}(a + \sum I, [1/b + \Lambda]^{-1})$$

where  $\Lambda = \sum_{s=t-\tau+1}^t \Lambda_s$  and  $\Lambda_s = \sum_{k \geq 1} w_k I_{s-k}$  is daily infectiousness.

### Value

A data frame with columns t, Rt\_mean, Rt\_lo, Rt\_hi (NaN where incidence is too low to estimate).

## References

Cori, A., Ferguson, N. M., Fraser, C. and Cauchemez, S. (2013). A new framework and software to estimate time-varying reproduction numbers during epidemics. *American Journal of Epidemiology*, 178(9):1505–1512.

## Examples

```
set.seed(1)
inc <- rpois(60, lambda = c(rep(50, 20), seq(50, 200, length=20),
                           seq(200, 30, length=20)))
rt <- cori_rt(inc, tau = 7, si_mean = 5.5, si_sd = 2.5)
plot(rt$t, rt$Rt_mean, type = "l", ylim = c(0, 4),
     xlab = "Day", ylab = expression(R[t]),
     main = "Cori-style Rt estimate")
abline(h = 1, lty = 2)
```

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npf\_seir

*Run the Nested Particle Filter for a stochastic SEIR model*

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## Description

Performs online Bayesian joint state and parameter estimation for the stochastic SEIR model with latent Ornstein-Uhlenbeck transmission dynamics, using the nested particle filter (NPF) of Crisan and Miguez (2018).

## Usage

```
npf_seir(
  observations,
  fixed,
  K = 100L,
  M = 200L,
  tau_outer = 0.3,
  x0 = NULL,
  seed = NULL,
  h_min = 0.01,
  h_max = 0.1,
  rho = 0.995,
  verbose = FALSE
)
```

## Arguments

observations	Numeric vector of length $T$ . Daily confirmed case counts $P_1, \dots, P_T$ .
fixed	Named list of fixed model parameters (see <a href="#">seir_simulate</a> ).
K	Integer. Number of outer (parameter) particles. Default 100.
M	Integer. Number of inner (state) particles per outer particle. Default 200.

tau_outer	Numeric in (0,1). ESS threshold for outer resampling. Outer resampling is triggered when $ESS_{outer} < \tau_{outer} \cdot K$ . Default 0.3.
x0	Numeric vector of length 5, or NULL. Initial state $(S_0, E_0, I_0, R_0, \Psi_0)$ . If NULL, derived from observations[1] via quasi-steady-state initialization; in that case the first observation is used only for initialization and excluded from the filtering updates.
seed	Integer or NULL. Random seed for reproducibility.
h_min, h_max, rho	Jittering bandwidth schedule parameters. The bandwidth at step $n$ is $h_n = h_{min} + (h_{max} - h_{min})\rho^n$ . Defaults: h_min = 0.01, h_max = 0.10, rho = 0.995.
verbose	Logical. Print progress every 50 steps. Default FALSE.

### Value

An object of class "npf\_seir", a list with components:

Rt\_mean, Rt\_lo, Rt\_hi Numeric vectors of length  $T$ . Posterior mean and 95%  $R_t = \beta_t S_t / ((\gamma + \delta)N)$ .

beta\_mean, beta\_lo, beta\_hi Posterior summaries for  $\beta_t$ .

theta\_mean Matrix of size  $T \times 3$ . Weighted posterior mean of  $\theta = (\kappa, \sigma_\Psi, \mu_\Psi)$  at each step.

final\_theta Matrix  $K \times 3$ . Outer particles at time  $T$ .

final\_w Numeric vector of length  $K$ . Outer weights at time  $T$ .

final\_inner List of length  $K$ . Final inner state particles used for posterior predictive simulation.

outer\_ess Numeric vector of length  $T$ . Outer ESS trace.

observations, fixed, call Input metadata.

### References

Crisan, D. and Miguez, J. (2018). Nested particle filters for online parameter estimation in discrete-time state-space Markov models. *Bernoulli*, 24(4A):3039–3086.

Feng, W. and Wang, W. (2025). Bayesian sequential inference for a stochastic SEIR model with latent transmission dynamics. *Preprint*.

### Examples

```
# Simulate and recover
fixed <- list(eps = 1/5, gamma = 1/10, delta = 1/(70*365),
             b = 1/(70*365), q = 0.3, N = 1e6, sigma_comp = 0.01)
x0 <- c(1e6 - 100, 50, 50, 0, log(0.25))
set.seed(1)
traj <- seir_simulate(200, kappa=0.05, sigma_psi=0.10,
                    mu_psi=log(0.25), x0=x0, fixed=fixed)
fit <- npf_seir(traj$obs[-1], fixed=fixed, K=50, M=100, seed=42)
plot(fit)
summary(fit)
```

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ou_params	<i>Compute exact Ornstein-Uhlenbeck discrete-time transition parameters</i>
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**Description**

For the continuous-time OU SDE  $d\Psi_t = \kappa(\mu_\Psi - \Psi_t) dt + \sigma_\Psi dW_t$ , the exact one-day transition is  $\Psi_n | \Psi_{n-1} \sim N(\mu_\Psi + \alpha(\Psi_{n-1} - \mu_\Psi), \tau^2)$  with  $\alpha = e^{-\kappa}$  and  $\tau^2 = \sigma_\Psi^2(1 - e^{-2\kappa})/(2\kappa)$ .

**Usage**

```
ou_params(kappa, sigma_psi)
```

**Arguments**

kappa	Positive mean-reversion speed.
sigma_psi	Positive continuous-time volatility.

**Value**

A named list with elements alpha and tau.

**Examples**

```
ou_params(kappa = 0.05, sigma_psi = 0.10)
```

---

plot.npf_seir	<i>Plot method for npf_seir</i>
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---

**Description**

Produces posterior summary plots for  $R_t$ ,  $\beta_t$ , or both.

**Usage**

```
## S3 method for class 'npf_seir'
plot(x, burn = 0L, which = "Rt", dates = NULL, ...)
```

**Arguments**

x	An npf_seir object.
burn	Integer. Number of initial steps to exclude from the plot.
which	Character. "Rt" (default), "beta", or "both" to show both trajectories in a two-panel display.
dates	Optional Date vector with one entry per observation to use as the x-axis.
...	Additional arguments passed to plot().

**Value**

Returns  $x$  invisibly. Called primarily for its side effect of producing a base-graphics plot. When `which = "Rt"` or `"beta"`, a single panel is drawn showing the posterior mean trajectory and 95% credible band. When `which = "both"`, a two-panel figure is produced showing  $R_t$  (top) and  $\beta_t$  (bottom).

---

predict.npf\_seir      *Posterior predictive forecasts from an npf\_seir object*

---

**Description**

Generates forward simulations from the filter's final filtered particles to produce a posterior predictive distribution over future case counts.

**Usage**

```
## S3 method for class 'npf_seir'
predict(object, horizon = 14L, n_draws = 1000L, ...)
```

**Arguments**

object	An npf_seir object.
horizon	Integer. Number of days ahead to forecast. Default 14.
n_draws	Integer. Number of Monte Carlo draws. Default 1000.
...	Ignored.

**Value**

A named list with components: `mean` (numeric vector of length `horizon`, posterior predictive mean), `lo` and `hi` (95%  $(n\_draws - horizon)$  matrix of Monte Carlo draws).

**Examples**

```
fixed <- list(eps = 1/5, gamma = 1/10, delta = 1/(70*365),
             b = 1/(70*365), q = 0.3, N = 1e6, sigma_comp = 0.01)
x0 <- c(1e6 - 100, 50, 50, 0, log(0.25))
set.seed(1)
traj <- seir_simulate(200, 0.05, 0.10, log(0.25), x0, fixed)
fit <- npf_seir(traj$obs[-1], fixed, K=50, M=100, seed=42)
fc <- predict(fit, horizon = 14)
print(fc$mean)
```

---

```
print.npf_seir          Print method for npf_seir
```

---

**Description**

Print method for npf\_seir

**Usage**

```
## S3 method for class 'npf_seir'
print(x, ...)
```

**Arguments**

```
x          An npf_seir object.
...        Ignored.
```

**Value**

Returns `x` invisibly. Called primarily for its side effect of printing a concise summary to the console, including the number of observations and particles, and the posterior means of the Ornstein-Uhlenbeck hyperparameters  $\kappa$ ,  $\sigma_\Psi$ , and  $\mu_\Psi$  at the final time step.

---

```
seir_simulate          Simulate a stochastic SEIR epidemic with latent OU transmission
```

---

**Description**

Generates a synthetic epidemic trajectory from the stochastic SEIR model with exact Ornstein-Uhlenbeck log-transmission dynamics, as described in Section 2 of Feng and Wang (2025).

**Usage**

```
seir_simulate(n_steps, kappa, sigma_psi, mu_psi, x0, fixed)
```

**Arguments**

```
n_steps      Integer. Number of days to simulate.
kappa        Positive numeric. OU mean-reversion speed.
sigma_psi    Positive numeric. OU continuous-time volatility.
mu_psi       Numeric. OU long-run mean of log-transmission.
x0           Numeric vector of length 5: initial state  $(S_0, E_0, I_0, R_0, \Psi_0)$ .
fixed        Named list of fixed model parameters. Must contain:
eps Incubation rate  $\epsilon$  (1/mean incubation period).
```

**gamma** Recovery rate  $\gamma$  (1/mean infectious period).  
**delta** Background mortality rate  $\delta$ .  
**b** Birth rate  $b$  (usually equal to  $\delta$ ).  
**q** Case detection probability  $q \in (0, 1]$ .  
**N** Reference population size  $N$ .  
**sigma\_comp** Compartment diffusion coefficient  $\sigma$ .

### Value

A data frame with  $n\_steps + 1$  rows (day 0 to day  $n\_steps$ ) and columns: day, S, E, I, R, Psi, beta ( $e^{\Psi_t}$ ), obs (simulated observed daily counts drawn from a Poisson distribution with mean  $q\epsilon E_t$ ).

### References

Feng, W. and Wang, W. (2025). Bayesian sequential inference for a stochastic SEIR model with latent transmission dynamics. *Preprint*.

### Examples

```
fixed <- list(eps = 1/5, gamma = 1/10, delta = 1/(70*365),
             b = 1/(70*365), q = 0.3, N = 1e6, sigma_comp = 0.01)
x0 <- c(S = 1e6 - 100, E = 50, I = 50, R = 0, Psi = log(0.25))
traj <- seir_simulate(n_steps = 200, kappa = 0.05, sigma_psi = 0.10,
                    mu_psi = log(0.25), x0 = x0, fixed = fixed)
plot(traj$day, traj$obs, type = "l", xlab = "Day",
     ylab = "Daily cases", main = "Simulated epidemic")
```

---

summary.npf\_seir

*Summary method for npf\_seir*

---

### Description

Summarises posterior parameter estimates and the range of  $R_t$ .

### Usage

```
## S3 method for class 'npf_seir'
summary(object, burn = 0L, ...)
```

### Arguments

object	An npf_seir object.
burn	Integer. Number of initial steps to exclude from summaries. Default 0.
...	Ignored.

**Value**

A named list of class "npf\_seir\_summary" returned invisibly with components:

theta Named numeric vector of length 3 giving the weighted posterior mean of the OU hyperparameters  $(\kappa, \sigma_{\Psi}, \mu_{\Psi})$  at the final time step.

ou Named list with elements alpha and tau, the exact discrete-time OU transition parameters derived from theta; see [ou\\_params](#).

The function is also called for its side effect of printing a formatted summary to the console, including posterior parameter estimates and the range of  $R_t$  over the retained time steps.

# Index

`cori_rt`, [2](#), [3](#)

`npf_seir`, [2](#), [4](#)

`npfseir` (`npfseir-package`), [2](#)

`npfseir-package`, [2](#)

`ou_params`, [2](#), [6](#), [10](#)

`plot.npf_seir`, [6](#)

`predict.npf_seir`, [7](#)

`print.npf_seir`, [8](#)

`seir_simulate`, [2](#), [4](#), [8](#)

`summary.npf_seir`, [9](#)